

$$f(x) = \frac{a_0}{2} + \sum_{n=1}^{\infty} (a_n \cos nx + b_n \sin nx).$$

La fonction est périodique de période T .

on sait que

si $0 \leq x \leq t$, $f(x) = \frac{x}{t}$

ou $t \leq x \leq T$, $f(x) = \left(\frac{1}{t-T}\right)x - \frac{T}{t-T}$

$$a_0 = \frac{1}{T} \int_0^T f(x) dx$$

$$a_k = \frac{1}{T} \int_0^T f(x) \cos kx dx$$

$$b_k = \frac{1}{T} \int_0^T f(x) \sin kx dx$$

$$a_0 = \frac{1}{T} \left[\int_0^t f(x) dx + \int_t^T f(x) dx \right]$$

$$= \frac{1}{T} \left[\int_0^t \frac{x}{t} dx + \int_t^T \left(\left(\frac{1}{t-T}\right)x - \frac{T}{t-T} \right) dx \right]$$

~~$$\frac{1}{T} \left[\int_0^t \frac{x}{t} dx + \int_t^T \left(\left(\frac{1}{t-T}\right)x - \frac{T}{t-T} \right) dx \right]$$~~

$$a_k = \frac{1}{T} \left[\int_0^t \frac{x \cos kx}{t} dx + \int_t^T \left(\left(\frac{1}{t-T}\right)x - \frac{T}{t-T} \right) \cos kx dx \right]$$

$$b_k = \frac{1}{T} \left[\int_0^t \frac{x \sin kx}{t} dx + \int_t^T \left(\left(\frac{1}{t-T}\right)x - \frac{T}{t-T} \right) \sin kx dx \right]$$