

$$\begin{aligned}
a) \quad & \sum_{i=1}^n (2i+3)^2 \\
&= \sum_{i=1}^n (4i^2 + 12i + 9) \\
&= 4 \sum_{i=1}^n i^2 + 12 \sum_{i=1}^n i + 9 \sum_{i=1}^n 1 \\
&= 4 \frac{n(n+1)(2n+1)}{6} + 12 \frac{n(n+1)}{2} + 9n \\
&= \frac{n}{6} (4(n+1)(2n+1) + 36(n+1) + 54) \\
&= \frac{n}{6} (4(2n^2+3n+1) + 36n+36 + 54) \\
&= \frac{n}{6} (8n^2 + 12n + 4 + 36n + 36 + 54) \\
&= \frac{n}{6} (8n^2 + 48n + 94) \\
&= \frac{n}{3} (4n^2 + 24n + 47)
\end{aligned}$$
